

DOOR ANGLE AS A FUNCTION OF TIME

- Q1** The angle increases from $t = 0$ to approximately $t = 1.45$. You can tell because the maximum value of the angle occurs at approximately $t = 1.45$.
- Q2** The maximum angle is approximately 106° , at $t = 1.45$.

THE DOOR AT TWO DIFFERENT TIMES

- Q3** The slider has a maximum value of 1. The smallest separation you can observe on the graph is about 0.01. The slider uses a logarithmic scale, so it's easy to achieve very small values—values that are much smaller than you can observe on the graph.
- Q4** Yes, the displayed values (to five decimal digits) continue to show the changes.

THE RATE OF CHANGE OF THE DOOR'S ANGLE

- Q5** The units are degrees/s. The rate of change tells you by how many degrees the door is opening or closing for every second.
- Q6** The rate of change is the slope of the dotted secant line. As the secant line approaches tangency, the calculated rate of change approaches the instantaneous rate of change.
- Q7** When the rate of change is positive, the door is opening; when the rate is negative, the door is closing. When the rate of change is close to zero, the door is moving slowly; when the absolute value of the rate of change is large, the door is moving quickly.
- Q8** When $t_1 = 1$ and $\Delta t = 0.1$, the calculated rate of change is 26.33629 degrees/s.

THE LIMIT OF THE RATE OF CHANGE

- Q9** The average rate of change is higher (more than 30 degrees/s) and appears to be a more accurate value for $t_1 = 1.0$.
- Q10** The rate of change appears to approach a limit; the differences are less and less. The rate of change seems to be approaching 30.685 degrees/s.

Instantaneous Rate

continued



.....

Q11 No, the change is too small to observe on the graph.

Q12 The derivative (that is, the limit of the rate of change) when t_1 is 3 seconds seems to be about -26.986 degrees/s. The negative sign means that the door is closing.