# **Balance Challenge**

#### Goals

- Identify weights of blocks from relationships shown by level pan balances.
- Replace variables or a group of variables with their values.
- Understand that substituting for one or more variables with others of equal weight will not affect the balance.

### Questions to Ask

- What is in the left pan of pan balance A? (1 cylinder and 2 cubes) How much do they weigh? (11 pounds)
- 2 What is in the right pan of B? (2 cylinders and 2 cubes) How much do they weigh? (14 pounds)
- 3 What do the left pan of A and the right pan of B have in common? (both have 1 cylinder and 2 cubes) What is different? (B has an extra cylinder.)
- How can you use that information to figure out the weight of the extra cylinder? (Replace the 1 cylinder and 2 cubes with 11 pounds, then remove 11 pounds from both pans. The extra cylinder is 14 11, or 3 pounds.)
- 5 What will you do after you know the weight of the cylinder? (Replace the cylinder in A with its weight in order to figure out the weight of the cube.)

#### Solutions

- 1.6
- **2.** 4
- **3.** 3
- 4. Possible solution: All of the blocks in the left pan of A are contained in the right pan of B. Replace the cylinder and 2 cubes in B with 11 pounds. Remove 11 pounds from each pan. Then the extra cylinder in B is 14 - 11, or 3 pounds. In B, replace each cylinder with 3 pounds. Remove 6 pounds from each pan. That leaves 2 cubes weighing 14 - 6, or 8 pounds. Each cube is 8 ÷ 2, or 4 pounds. Replace the cylinder in C with 3 pounds and the cube with 4 pounds. Then remove 7 pounds from each pan. The sphere weighs 13 - 7, or 6 pounds.

## f.y.i.

Once students have identified the group of blocks that are the same in two pans of two different balances, have them draw a circle around them. In this way, they can more easily see what is "extra" in one of the pans.

Some students may notice that in B there are two pairs of blocks with a cylinder and cube in each. Thus the weight of each pair is  $14 \div 2$ , or 7 pounds. The same pair of blocks in A can be replaced with 7 pounds. The weight of the "extra" cube in A can then be determined.

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