

Minnesota Reveal
MATH®

Reveal the Full Potential
in Every Student



Reveal the Mathematician in Every Student

Minnesota Reveal Math® helps students develop the positive mindset, confidence, and skills to become problem solvers and mathematical thinkers. The program works by incorporating both inquiry-focused and teacher-guided instructional strategies within each lesson. Informed by the latest research on how they learn best, *Minnesota Reveal Math* ensures students don't just meet the standards—they master them!

Our Powerful Program:



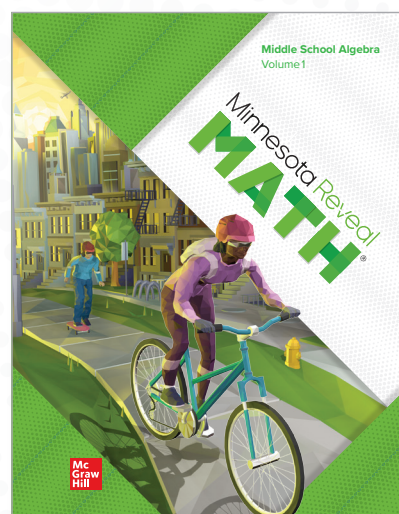
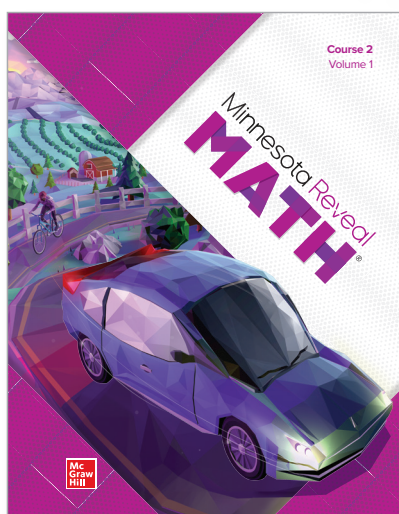
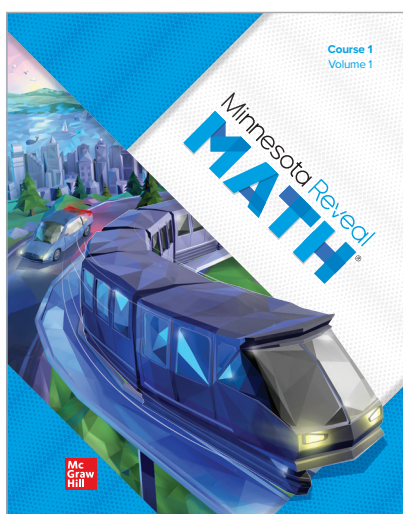
Champions a positive classroom centered on curiosity, connection, and a mathematical mindset.



Offers a flexible lesson design that provides access to rigorous instruction with robust teacher supports and scaffolds.



Tailors instruction for each student through data-driven insights and purposeful, personalized differentiation.



Minnesota Reveal Math Authorship

McGraw Hill learning scientists teamed up with expert authors to create a program guided by validated academic research and classroom best practices.



Sarah Bush, Ph.D.

Expert in both theory and practice for middle school math instruction



John SanGiovanni, M.Ed.

Leader in understanding the mathematics needs of students and teachers



Annie Fetter

Advocate for student ideas and thinking that foster strong problem solvers



Cathy Seeley, Ed.D.

Thought leader and facilitator of high-quality mathematics education for all



Linda Gojak, M.Ed.

Expert in both theory and practice of strong mathematics instruction



Raj Shah, Ph.D.

Champion of perseverant problem-solvers and student curiosity in mathematics



Christa Jackson, Ph.D.

Advocate for strong STEM education and equity for middle school students



Cheryl Tobey, M.Ed.

Facilitator of strategies that drive informed instructional decisions



Georgina Rivera, M.Ed.

Expert in building student agency through culturally responsive teaching



Dinah Zike, M.Ed.

Creator of learning tools that make connections through visual-kinesthetic techniques



George Roy, Ph.D.

Expert in integrating technology into middle school instruction

Program Design Influenced by Teachers, Research, and Industry Experts

To design the program, our expert authorship consulted rigorous educational research. Foundational texts include *Principles to Actions* (NCTM) and *Making Sense of Math* (Cathy Seeley) as well as learning models such as Bloom’s Taxonomy and Webb’s Depth of Knowledge Guide. We then called upon our most trusted collaborators, hundreds of teachers across the country, for instructional insights to bring this research to life.

Major Focus Areas:

A Supportive Classroom Culture for All Students

Learner-focused practices develop a classroom designed for equitable learning.

Rich Mathematical Discourse

Instructional options and supports focus on student discourse while emphasizing academic and math vocabulary.

Productive Struggle

Opportunities to explore and engage with challenging mathematical ideas and relationships build deep understanding.

Sense-Making

Support for the development of sense-making and critical thinking skills develops proficient problem solvers.

Fluency

Flexible strategies help students to practice math content and achieve automaticity.

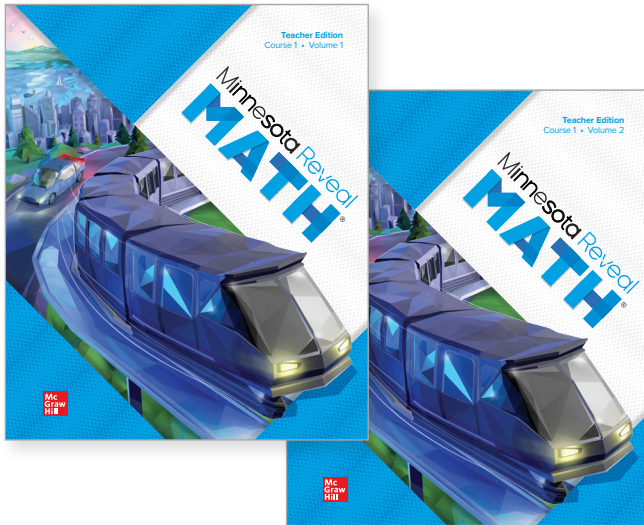
Instructional Routines

Structures and expectations create productive classroom interactions with students. Read more about Math Language Routines (MLR) on page 17.

Metacognition

Student reflection promotes math learning.

Teacher Resources



Print Resources

Teacher Edition, 2 Volumes

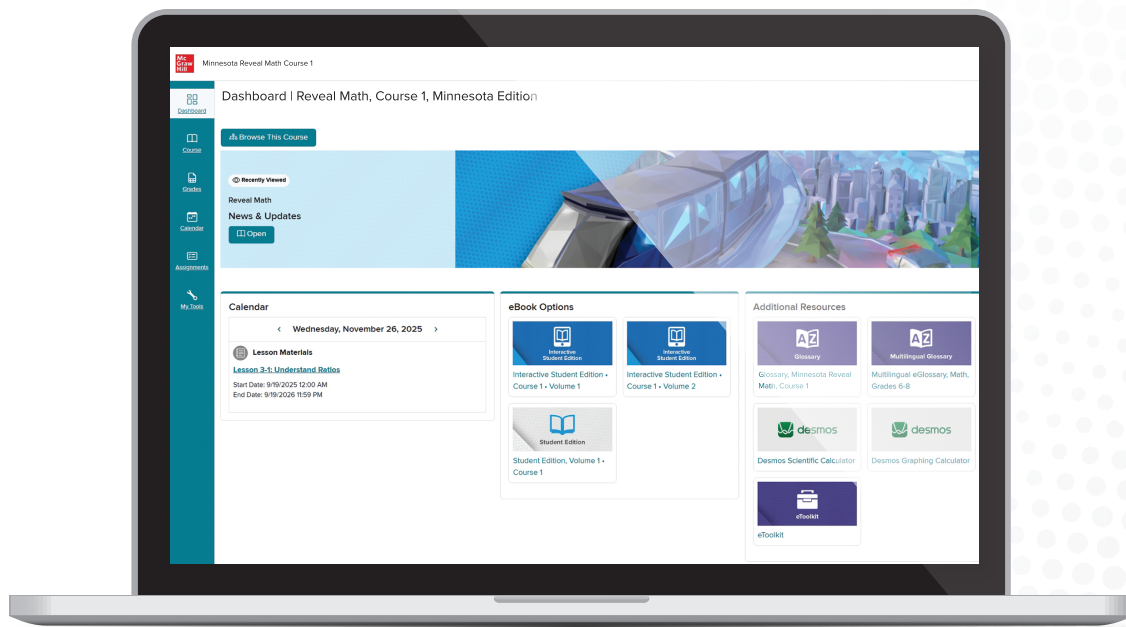
These spiral-bound Teacher Editions provide the essentials to plan and implement high-quality math instruction. Inside, you will find instructional supports including NCTM's Effective Teaching Practices, Math Language Routines, Multilingual Learner (ML) Language Scaffolds, and differentiation recommendations.



Digital Teacher Center Resources

Teachers have access to an intuitive and easy-to-use platform for planning, teaching, and assessment. The teacher digital experience includes:

- Engaging, interactive, prebuilt lesson presentations with embedded technology.
- Editable lesson presentations in PowerPoint allowing teachers to customize and share slide content or teach offline.
- An expansive library of professional learning workshops and videos, including expert insight videos.
- Digital practice and assessments item banks to build custom assignments.
- A robust selection of engaging differentiation resources.
- Dynamic unit practice.
- Digital exploration activities powered by Web Sketchpad®.
- Anytime access to the eToolkit.
- Practice and assessment PDFs.
- Teacher and administrator data and reporting.
- Classroom management and grouping tools.
- The ability to add resources, including presentations and website links.



Student Resources



Print Resources

Student Edition, 2 Volumes

Available in print and interactive formats, the Student Editions are write-in, three-hole-punched, and perforated for easy organization in a binder. Students engage in learning through the use of problem-solving, discourse, and reflection.

Digital Student Center Resources

Students have access to a robust set of engaging digital tools and interactive learning aids, including:

- An Interactive Student Edition.
- Daily, interactive practice with embedded learning aids and dynamic (algorithmic) items.
- Dynamic, exploratory activities powered by Web Sketchpad®.
- Anytime access to a robust eToolkit (Virtual Manipulative Suite).
- Rich, exploratory STEM Adventures.
- Online assessments with interactive item types.
- Math Replay videos to review lesson content.
- Digital games designed for purposeful practice.

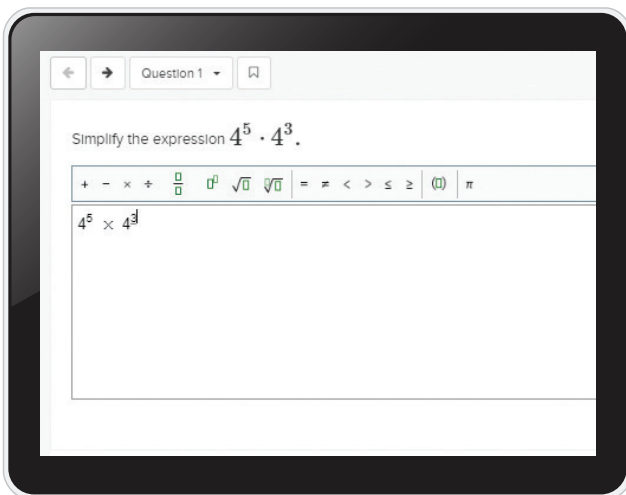
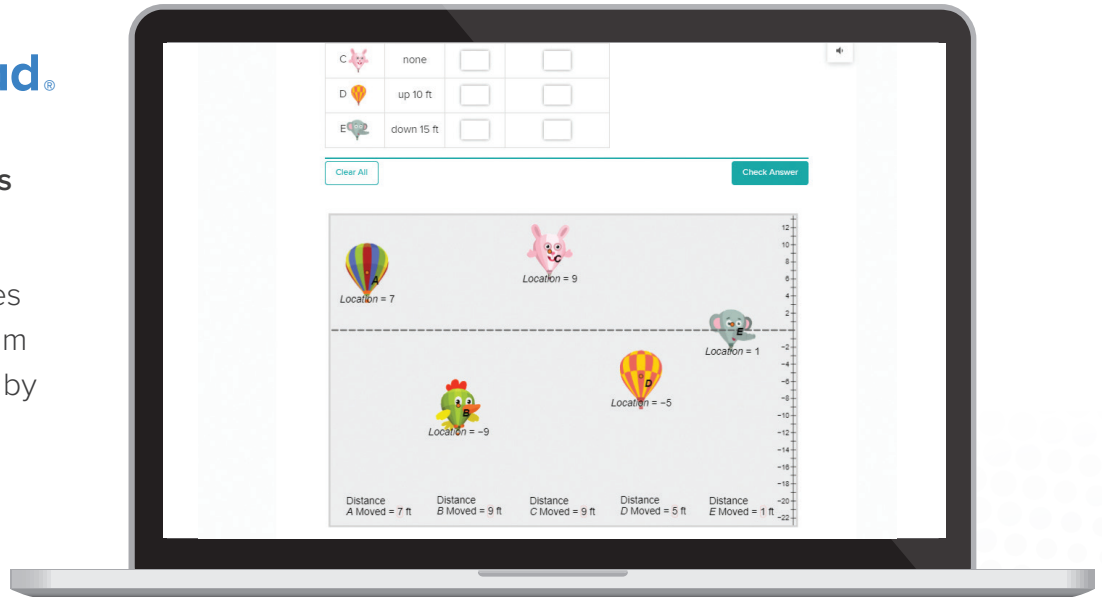
Where Technology Meets Math

Minnesota Reveal Math® supports both low-tech and high-tech classrooms. The blended print and digital instructional model captures the best of both modalities and brings them together in a seamless experience that makes math meaningful for your students.



Visualize Math Concepts in Action

Web Sketchpad® activities included with the program enhance understanding by demonstrating dynamic math concepts.



Prepare Students for Computer-Based Testing

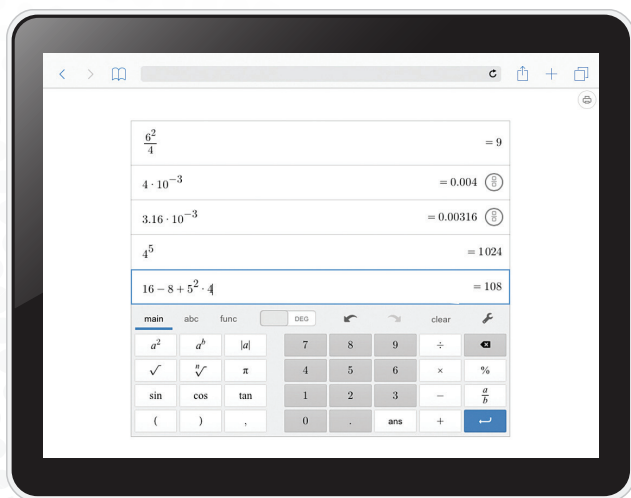
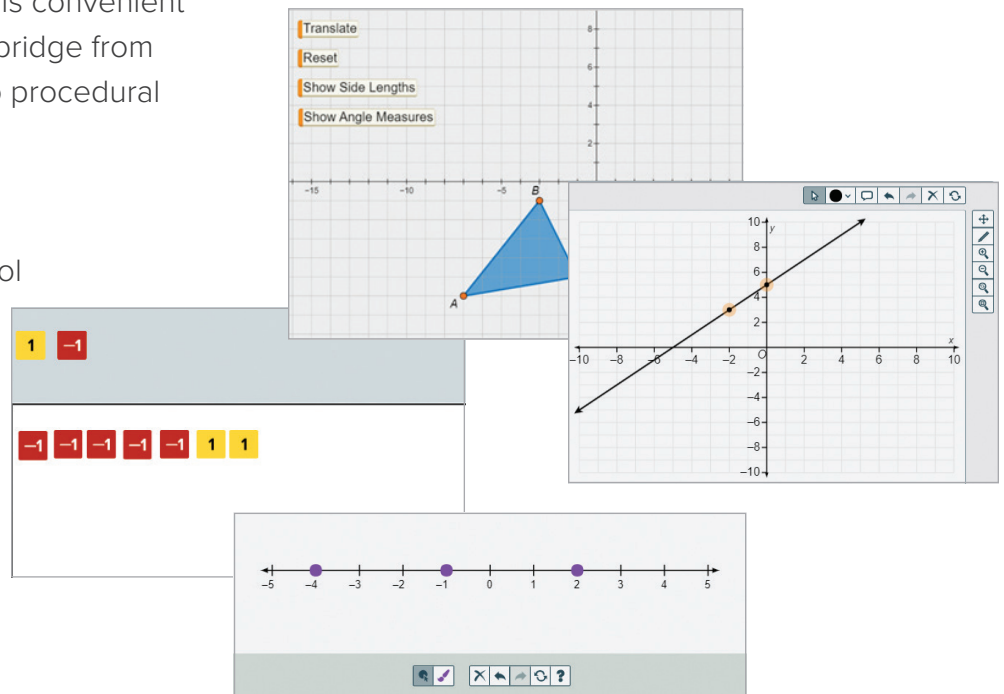
Technology-enhanced items provide students the valuable practice they need to master computer-based assessments. These items include:

- Drag-and-drop
- Equation editor problems
- Multiselect
- Open response

Utilize Digital Tools for Problem Solving

Embedded within lessons, this convenient collection of eTools builds a bridge from conceptual understanding to procedural fluency. It includes:

- Number Line Tool
- Coordinate Graphing Tool
- Transformations Tool
- Algebra Tiles Tool



Explore, Model, and Apply Math

The best-in-class Desmos scientific calculator, easily accessible in *Minnesota Reveal Math*, allows students to practice using the same resource that appears on many common standardized tests.

Motivate with Truly Enjoyable Technology

Designed with student engagement in mind, the digital resources in *Minnesota Reveal Math* include animations, videos, and interactive problems to enhance context and learning.



Champion a Positive Classroom

Engaging students' interest in mathematics at the middle school level helps learners see themselves as problem solvers and doers of mathematics, both of which are critical for achieving academic success.

Build Student Agency

Building agency is integral to helping students take ownership of their learning. With ownership, students are more willing to make mistakes and seek creative solutions to mathematical problems.

Encourage Growth Mindset

Math is... **Mindset**

Why is it important to explain your thinking clearly and concisely?

Mindset Matters tips at the beginning of each unit provide strategies for encouraging a growth mindset and productive approaches to problem solving.

Establish a Community of Learners

The Math is... Unit helps students and teachers focus on math as a set of problem-solving strategies instead of an end result. In this unit, students work together to define a productive and positive classroom environment where all students can:

- Share and exchange ideas.
- Collaborate to solve problems.
- Find success and build confidence in mathematics.
- Take ownership of learning.
- Become creative problem solvers.

Math is...

Sharing and Growing Together

LESSON 1-4
Math is In Explaining and Sharing

LESSON 1-5
Math is Finding Patterns

LESSON 1-6
Math is Ours

Lesson Highlights and Key Takeaways

In this lesson, students discuss what a productive learning environment is for math. They describe the qualities and attributes of this classroom setting and work as a class to decide on classroom norms that create this productive setting.

- Students describe the attributes of a productive learning environment for mathematics.
- Students develop a set of classroom norms to establish and maintain a productive learning setting.

Math Background

The lesson focuses on establishing a productive math learning environment in which all students feel encouraged to participate. Such a learning environment requires a commitment on everyone's part to agree to and follow the classroom norms for respectful and productive interactions and collaborations. It also requires a commitment from everyone to support one another's learning needs and preferences. That might mean allowing students to work independently in some instances while others work in groups.

Depending on students' earlier experiences learning math, they may or may not have positive dispositions towards math and may or may not look forward to math class. Fostering a sense of community and respect among all can sometimes help motivate all students to participate more in math class.

Teacher Edition Math is... Lesson Opener pages

Summarize: Math is Ours

We are a community of math thinkers and doers. Sharing our math strengths with others helps us grow. Learning about the math strengths of others can help us grow, too.

When we do math as a community,

- we often work together.
- we sometimes work on our own.
- we show respect and consideration for our classmates and our community.
- we show respect for ourselves and our math ideas.

Apply: Community Agreements

Communities often have agreements that all members of the community must agree to in order to be a part of the community.

Question What ideas do you recommend that the whole class agrees to so that math class is a community of learners?

Answer the question in the space below.

Math is Done with Others

How do we do math as a community?

When we do math, we often work together.

When we work together, we collaborate and support each other.

- We listen attentively to classmates.
- We share our thinking.
- We are respectful of others' ideas.
- We critique the ideas of others, not our classmates.
- We take turns when sharing ideas.

When we do math, we sometimes work on our own.

- We stay focused on our work.
- We seek help when we are stuck.
- We respect our classmates' boundaries and work habits.
- We avoid interrupting our classmates unnecessarily.

Let's Explore More

a. What skills and knowledge do you bring to a group that helps it be successful?

Summarize: Math is Mine

We are all doers of math and use math in our daily lives in ways that we may not realize. We all may do math differently. Sharing our math strengths with others helps us grow. Learning about the math strengths of other can help us grow, too.

Apply: A Sense of Belonging

We all have a need to feel like we belong to a community. Think about the different communities that you belong to.

Question What makes you feel like you belong to these different communities?

Complete the table below.

Community that I belong to	What I like about being in that community	How I feel when in that community	How ideas about that community apply to our math community

Student Edition Math is... activities build confidence, promoting student agency and collaboration.

Spark Curiosity and Problem-Solving



Raj Shah, Ph.D.

Contributing Author



Curiosity Makes Math Irresistible

Making math irresistible for students starts with sparking their interest and curiosity. Each *Minnesota Reveal Math*[®] unit has a unit topic that students explore through the Unit Opener and the Ignite! activity.

Ignite! activities are collaborative activities designed by *Minnesota Reveal Math* contributing author Raj Shah, Ph.D., to engage students and spark their mathematical curiosity prior to starting a unit. In each unit, the Ignite! activity:

- Follows a theme that relates to the STEM scenario in the Unit Opener.
- Poses interesting questions to motivate students to problem solve.
- Supports productive struggle and facilitates discourse.
- Recurs at the end of the unit as part of the Mathematical Modeling task.

Name _____ Date _____ Period _____

IGNITE!

Determining the U.S. Population

Every ten years since 1790, U.S. Government has conducted a census. At that time, census takers visited every house in the U.S. States to record the number of people living in the house.

For exercises 1-4, answer each question.

1. How might the methods used to conduct the census have changed since 1790?
2. What could be one method conducting a census of the people in your school?
3. Would the same method work for conducting a census of the people in your city or town? Explain your thinking.
4. You are part of a team creating a new school council for your school that includes everyone in the school—students, teachers, staff, and administrators. What would you propose for deciding the number of representatives each group would have? Explain your thinking.

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Bring the World Into Focus Through STEM

With STEM-focused unit topics, *Minnesota Reveal Math* helps students observe and understand the math taking place all around them.

- Students engage in rich, contextual problem-solving tasks to explore real-world concepts.
- Modeling tasks help students apply the math they know to solve problems in their everyday lives.


Think About It

Under what conditions would air purification be necessary?

Unit 3
Proportional Relationships

Essential Question
How can you determine proportionality between two varying quantities?

Explore Through STEM
Air in Flight
Airlines have systems in place to create a healthy cabin environment for their passengers where the air is replaced every few minutes. Filters are used to prevent viruses and bacteria from spreading. The air flow design has most air leaving the cabin in the same row in which it enters the cabin.



Think About It
Under what conditions would air purification be necessary?

Unit Opener

Essential Question
• How can you determine proportionality between two varying quantities?
Encourage students to share their initial responses to the Essential Question. Because students have not yet been formally introduced to proportional relationships, they may not have much to share. Then revisit the question throughout the unit, and ask students to expand on or revise their initial responses.

Explore Through STEM
Air in Flight
Throughout this unit, students will explore the proportional representation that informs the use of air sensors and air purifiers. Have students notice and wonder about the image. Ask:
• How are the passengers on the plane able to breathe when flying at high altitudes?
• How could we ensure we have enough oxygen for all the passengers on a long flight?
• How might we determine the air is safe to breathe on an aircraft?

Think About It
Under what conditions would air purification be necessary?
To facilitate discussion, use these prompts:
• How might an airline determine how much air circulation is needed on a given flight?
• How might air be evaluated and purified throughout a flight?
• What might be limitations to ensuring air quality on an aircraft? When might air sensors and purifiers not be effective?
Consider having students think about whether the size of the aircraft changes the amount of air circulation needed on the flight. They could explore what considerations need to be made for different numbers of passengers on various flights.

Preparing for the Explore and Discuss
How Do I Choose?
To decide which exploration to implement, consider the **Activity-Based Explorations (ABEs)** are designed to engage students in deep understanding and research-based teaching practices. In Lessons 3-1 and 3-5 offer unique learning opportunities.
• Students are introduced to the concept of proportionality in Lesson 3-1. The ABE for this lesson is designed to dig into what a proportion is and how it is used to solve problems.
• In Lesson 3-5, students explore tools to represent proportional relationships. The ABE is designed to explore how these tools make the relationship between quantities more clear.
• Consider the grouping of students who are working on these tasks. Because students are expected to work in groups, plan groups of students to provide the opportunities for everyone in the group to engage in the work.

Teacher Supports for Rich STEM Discourse

A teacher facilitation guide within the Teacher Edition supports rich discourse around the STEM topic of each unit, including visuals and prompts, as part of the Unit Opener. Available both in print and online formats of the Teacher Edition!



Flexible Lesson Design

Balanced Instructional Design

Minnesota Reveal Math[®] was built to align with the three pillars of a high-quality mathematics curriculum: focus, coherence, and rigor. This intentional instructional design ensures that students develop deep understanding, make connections, build conceptual proficiency, and understand the “why” behind mathematics.

Lesson are designed with three main learning objectives: content, language, and Math Mindset. To ensure coherence, there is a well-defined learning progression that builds upon previous lesson content and anticipates future lessons. Additionally, each lesson prioritizes one or more aspects of rigor that align with content standards.

FOCUS	COHERENCE	RIGOR
Math Objectives	Previous	Conceptual Understanding
Language Objectives	Now	Procedural Skill & Fluency
Math Mindset Objectives	Next	Application

Instructional Choice

Minnesota Reveal Math 6–8 offers teachers two instructional options: **Activity-Based Exploration** and **Guided Exploration**. They can choose whichever best meets the learning and pedagogical needs of their students and their instructional preferences.

Explore – Session 1 15–20 min

Launch Explore Assess Practice

CHOOSE YOUR OPTION

Activity-Based Exploration

Dividing with Fractions and Whole Numbers

Implement Tasks That Promote Reasoning and Problem Solving
Students explore using models to divide whole numbers by fractions and fractions by whole numbers.

Materials
Digital: *Activity Exploration Journal*, pp. AEJ1–AEJ2, 1 per student
Hands-On: ruler or straightedge, 1 per pair; *Activity Exploration Journal*, pp. AEJ1–AEJ2, 1 per student

Directions
Have students respond to the **Introductory Question** in their *Activity Exploration Journal*.
How can you use models to divide whole numbers and fractions?
Group students in pairs or small groups to work on this activity.

- Today we will explore dividing with whole numbers and fractions.

Digital: Students move tape diagrams and use the tools to divide rectangles. Using WebSketch™, students use models to explore division with fractions and whole numbers.
Hands-On: Student-pairs draw models to solve the trail mix division problems.

Support Productive Struggle
As student-pairs explore the activities, check that all pairs understand the task. If students need guidance or support, ask:

- What's the same and what's different about the different models?
- How does representing each problem with a model help you understand the problem?

Math is... Using Representations

- How can you use a picture to model the problem?

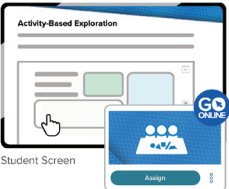
Entering/Emerging Have students consider how they can model the problem with a picture. Ask volunteers to share how a visual representation helps them understand the problem. Have students complete the **Concluding Questions** in their *Activity Exploration Journal*.

- How can you divide a whole number by a fraction?
- How can you divide a fraction by a whole number?

Multilingual Learner Scaffolds
Entering/Emerging Use the activity, circulate and explain the activity, circulate and explain the activity, circulate and explain the activity.

Developing/Expanding Use of model as an adjective. As students circulate and have orally explain the frames such as I can see this model shows.

Bridging/Reaching Concluding Questions use the words they in their responses.



Exploration pages in the Teacher Edition

Guided Exploration

STEM Camp

Students explore using a model to divide a whole number by a fraction.

Materials
ruler or straightedge, 1 per student-group (optional)

Introduce the problem situation on Student Edition p. 8.

Pose Purposeful Questions

- How are fractions used in this problem?
- What operation does the model for this problem represent?

Math is... Using Representations

- How can you use a picture to model the problem?

Ask students how they can represent the quantities given in the problem with a picture. Have volunteers share how a visual representation helps them understand the problem.

Collaborate and Connect

- How can you use the tape diagram to determine how many $\frac{3}{4}$ -hour parts are in 3 hours?

Have students work in pairs to discuss the tape diagram and shade in groups of three-fourths. Students can use the ruler or straightedge to draw their own tape diagrams to represent the problem situation. Give groups a chance to share how they shaded in the models. Discuss with students how they can differentiate between each group of three-fourths so that they will know how many groups are in 3 hours.

Let's Explore More

Co-Craft Questions and Problems: Co-Craft Problems

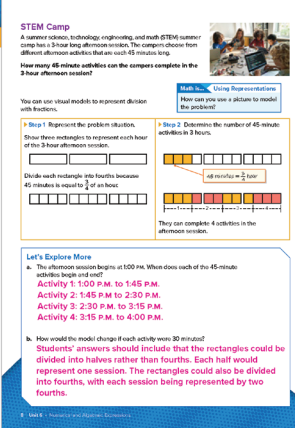
- Create:** Pair students and have them co-create a problem similar to the STEM Camp problem.
- Solve:** Have students work together to solve their problem before trading them with another pair.
- Exchange:** Have students trade their problem with another pair and solve. Next have them form a small group with the same pair. The small group checks solutions and methods and corrects any mistakes.
- Topic Support:** Before pairing students, you may want to brainstorm with the entire class different ways to partition one hour.

Check that students understand that they can use models in the same way to solve problems involving different fractions. Encourage students to write a division expression that represents the problem before solving.

Multilingual Learner Scaffolds
Entering/Emerging Display and pronounce *minute, hour, fourths, and quarter*. Using visual representations of digital and analog clocks, show how minutes and hours are represented. On the analog clock, use shading to show that one-fourth of an hour is a quarter of an hour. As needed, use the Spanish cognates *minuto, hora, and cuarto*. Then, have students label their clocks and fractions of an hour.

Developing/Expanding Confirm students' understanding of the words *activities, sessions, and models*. Clarify the spelling change between *activity* and *activities*. Demonstrate the use of model as a noun and a verb. Have students use these terms to restate the problem situation in their own words.

Bridging/Reaching Have students use the words *convert* and *conversion* in their responses.



Student Edition, p. 8

Effective Teaching, Active Learning

Effective Teaching Practices provide opportunities for teachers to elicit and use evidence of student thinking to help target their instruction effectively. Understanding student reasoning by asking them to explain their answers allows teachers to reinforce and enhance student understanding or target and address misconceptions.

Concept exploration, collaboration, and choice of problem-solving strategy help students develop and exercise agency during learning. Additionally, students begin to understand that mathematics is a language of its own in which they can communicate effectively to deepen their understanding.

ETP Effective Teaching Practices

Elicit and Use Evidence of Student Thinking

As students progress through the unit, ask them to explain their reasoning. Understanding the reasoning for their answers—whether they are correct or incorrect—allows for targeted instruction to reinforce and expand or enhance their understanding or address misconceptions and misunderstandings in a timely way.

As students learn about proportionality, there are multiple possibilities for errors in execution. Students may have misconceptions about

- the difference between proportional and nonproportional relationships;
- linear graphs that do not pass through the origin;
- common factors that define equivalent ratios and proportions.

Ask frequent questions, especially those that require reasoning. Use students' responses to inform instruction and determine what kinds of practice and review might be necessary.

For example, if students struggle to determine equivalent ratios or to identify the constant of proportionality, spend some time revisiting multiplication and division of fractions.

In Lessons 3-3, 3-4, and 3-5, students are introduced to proportional relationships. Monitor closely students' responses and thinking in these lessons to ensure they are understanding proportional relationships accurately.

Develop - Session 2 10-12 min

Launch Develop Summarize & Apply Assess Practice

Continue with your selected option from Session 1.

Activity-Based Exploration

Activity Debrief

3.3 Stronger and Clearer Each Time: Successive Pair Share

1. **Think Time:** Give students 5-10 minutes to review their responses to the **Concluding Questions** from the previous session and to think about what they will say to their first partner to explain and justify their responses.
2. **Structured Pairing:** Using a successive pairing structure, students explain their responses to at least two different partners. Each time, the student speaking focuses on explaining their reasoning clearly and precisely. The student listening asks clarifying questions to help their partner to be clearer and more precise in their communication.
3. **Post-Write:** Students revisit and revise their responses to the **Concluding Questions** as needed.

ETP Elicit Evidence of Student Thinking

As students complete the **Stronger and Clearer Each Time**, listen for students' understanding of:

- how to solve division problems in which a whole number is divided by a fraction or a fraction is divided by a whole number.
- the difference between models used to divide a whole number by a fraction or a fraction by a whole number.

ETP Facilitate Mathematical Discourse

Facilitate a whole-class discussion of the activity. Using the evidence of student thinking that you gathered, sequence students' sharing of findings to highlight different approaches and thinking strategies used to respond to the **Concluding Questions**.

- How can you divide a whole number by a fraction?
- How can you divide a fraction by a whole number?

During the whole-class discussion, connect students' understanding of division with fractions and whole numbers to these new key terms and concepts:

- An equation can also be used to divide with fractions and whole numbers.
- You can multiply the dividend by the reciprocal of the divisor to find the quotient.
- A reciprocal is one of a pair of numbers whose product is 1.

Math Is... Asking Questions

- What questions can you ask to better define a problem involving division expressions with fractions and whole numbers?

3.3 Encourage students to think of questions they can ask before working through a division problem involving fractions and whole numbers that would help them to solve, regardless of the quantities involved.

3.3 Multilingual Learner

Entering/Emerging To prompt debrief from the previous session, students to write words and can use when speaking with. Provide a word bank that includes equation, expression, equivo and represent.

Developing/Expanding As students move from one partner to the next, listen to questions their first partner and then try to think of a different question they want to ask their partner. When they revise their responses, have them focus on clarity.

Bridging/Reaching Have students clarify questions to understand their responses. Have students include questions or from their partners in their responses.

ETP Elicit Evidence of Student Thinking

As students complete the **Stronger and Clearer Each Time**, listen for students' understanding of:

- how to solve division problems in which a whole number is divided by a fraction or a fraction is divided by a whole number.
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Language of Math

Help your students develop the language of math with *Minnesota Reveal Math*[®] Math Language Routines and comprehensive vocabulary support. These embedded resources support teacher facilitation and student acquisition of mathematical language and vocabulary.

MLR Collect and Display

As students discuss the questions, listen and write on the board any key words they use. Display the words and phrases for student reference. Use the student-generated expressions to help make connections between student language and math vocabulary. Update the collection with new understandings as the lesson progresses.

Math Language Routines provide a framework for teachers to seamlessly promote mathematical language development as part of their everyday instruction to support all types of learners.

LOM Language of Mathematics

Vocabulary

Students will be using these key terms in this unit.

- **Constant of proportionality** (Lessons 3-2, 3-3, 3-4, 3-5): This is a new term. Students may be familiar with the term *constant* describing a situation that occurs continuously over a period of time. The mathematical meaning in this context is similar—it describes a quantity or parameter that does not change. The *constant of proportionality* describes the relationship that does not change between values in two sets of values. See entry for proportionality.
- **Constant ratio** (Lessons 3-2, 3-3, 3-4, 3-5): This is a new term. Students were introduced to the term *ratio* in Grade 6 during their study of ratios and rates. They determined equivalent ratios to solve problems during their Grade 6 study. The *constant ratio* describes the ratio that can be used to determine equivalent ratios.
- **Origin** (Lesson 3-7): Students were introduced to this term in Grade 5 when they were introduced to the coordinate plane.
- **Proportional relationship** (Lessons 3-1, 3-2, 3-3, 3-4): This is a new term. A proportional relationship is one for which all the values in two sets are equivalent ratios.
- **Proportionality** (Lessons 3-2, 3-3, 3-4, 3-5): This is a new term. A proportionality indicates equality between two or more ratios.
- **Ratio** (Lessons 3-1, 3-2, 3-3, 3-4, 3-5, 3-6): Students were introduced to this term in Grade 6 during their study of ratios and rates.
- **Unit rate** (Lesson 3-1, 3-4, 3-5): Students were introduced to this term in Grade 6 during their study of ratios and rates.

Building the Language of Mathematics

As students work through each lesson, have them complete the graphic organizer to build understanding of and proficiency with key mathematical terms and concepts.

Encourage students to come up with their own definitions and descriptions of terms. When students generate their own definitions or descriptions of terms, they are more likely to remember them long term.



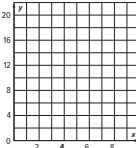
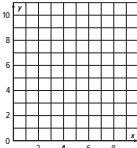
Word Wall

If there is a Math Word Wall in the classroom, ask students to add their words, examples, and counterexamples of proportional relationships to the wall. As they share them, have each student explain their entry.

Building the Language of Mathematics

Complete the graphic organizer as you work through the unit.

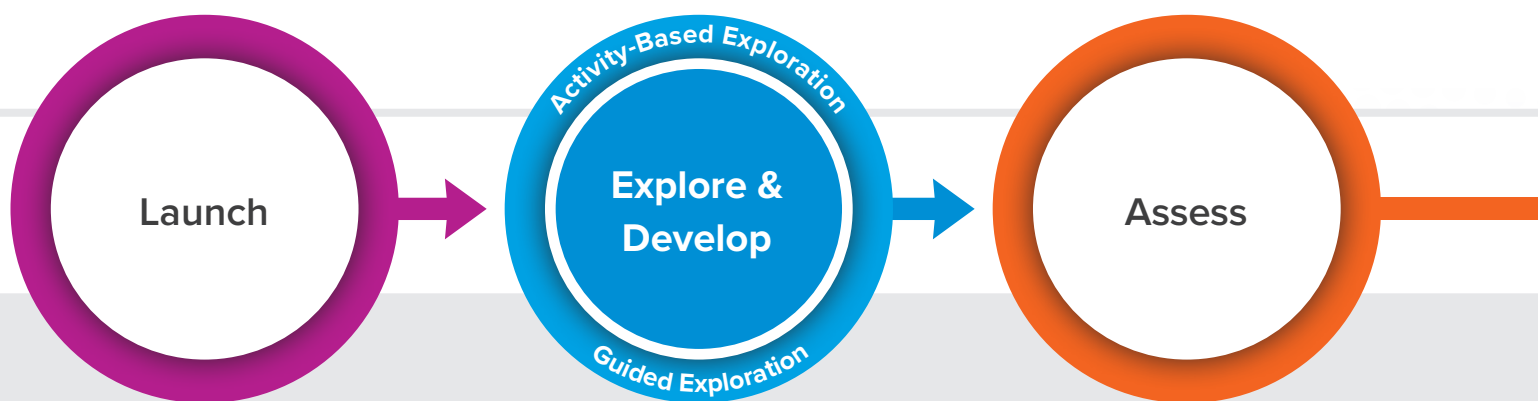
Proportional Relationships

Way to Represent	Example	Non-example
Table		
Graph		
Equation		



Lesson Model

The *Minnesota Reveal Math*[®] lesson model keeps sense-making and exploration at the heart of learning. Lessons offer **two instructional options** to develop the math content and tailor the instruction to students' learning needs.



Be Curious, a sense-making activity:

- Students focus on noticing and wondering, not problem-solving.
- Teachers foster students' thinking through meaningful discussion.

Explore & Develop unpacks the lesson content through either an Activity-Based or Guided Exploration:

- Students explore concepts in small groups during which they can formalize their emergent ideas.
- Teachers facilitate the exploration of concepts through rich discourse.

Minnesota Reveal Math lessons offer two opportunities to gauge student learning:

- The **Exit Ticket** is completed after Session 1 and helps to inform instruction for Session 2.
- The **Lesson Quiz** is completed after Session 2 and helps inform differentiation.

Create Consistency in Learning

Instructional routines are embedded within *Minnesota Reveal Math* lessons to help students become proficient doers of mathematics.

Build Fluency

Number Routines

Support the development of flexibility with numbers and fluency with operations.

MLR

Math Language Routines

Promote mathematical language development as part of instruction.



Sense-Making Routines

Build sense-making as a foundation for problem-solving and mathematical modeling.



The **Practice** pages offer students opportunities to engage with the math and reflect on their learning:

- Students practice lesson concepts by completing the exercises.
- Teachers monitor progress and have students reflect on the lesson learning targets.

Lesson **Differentiation** supports all students in their path to understanding:

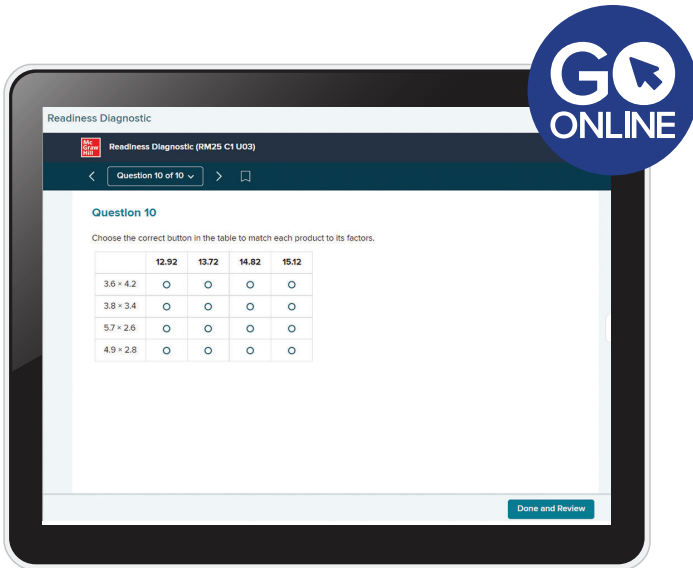
- Students work on differentiated tasks to reinforce their understanding, build their proficiency, and/or extend their thinking.

Types of Differentiation

- R Reinforce Understanding**
Resources designed to revisit lesson concepts.
- B Build Proficiency**
Resources to build proficiency with lesson skills.
- E Extend Thinking**
Resources to enrich lesson concepts.

Readiness Diagnostic

Before beginning the unit, students complete the **Readiness Diagnostic** to identify any learning gaps. The diagnostic can be delivered online or downloaded and printed.



Online Diagnostic




Print Diagnostic

Provide Targeted Intervention

The Teacher Edition includes an **Item Analysis** table which recommends **Guided Support Intervention Lessons** for students who need them. These lessons are assignable through the Digital Teacher Center.

Targeted Intervention

 Use Guided Support intervention lessons available in the Digital Teacher Center to provide targeted intervention.

Item Analysis

Item	DOK	Skill	Guided Support Intervention Lesson
1	1	Count to 3	Count to 3 with Dots as Objects
2	1	Represent 5	Identify Sets of 1 to 5 Objects
3	3	Compare groups	Same or Different with Two Groups
4	2	Count to 3	Count to 3 with Dots as Objects
5	2	Compare numbers	Less than, Greater than, or Equal to 5
6	1	Represent 3	Identify Sets of 1 to 5 Objects

STEM Connections

Explore unit concepts through recognizable STEM scenarios.

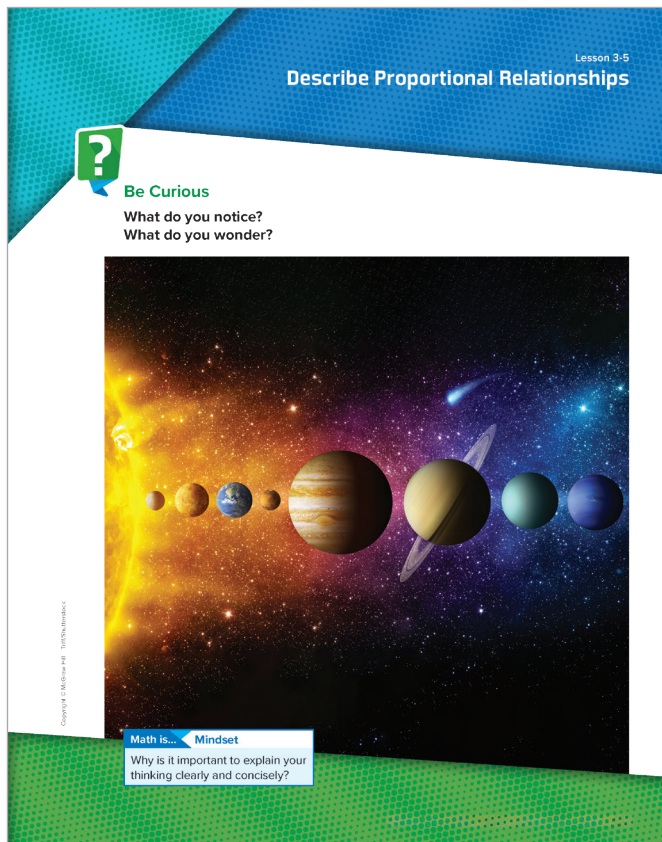
- **Explore Through STEM** identifies a STEM scenario in the Unit Opener that sets the theme that will be revisited throughout the unit.
- **STEM Adventures** are digital activities where students can engage in experiments, make hypotheses, and apply mathematical knowledge to analyze data.
- The **Mathematical Modeling** tasks at the end of each unit tie back to the STEM scenario in the Unit Opener.



Use Questions to Promote Student Ideas

Be Curious

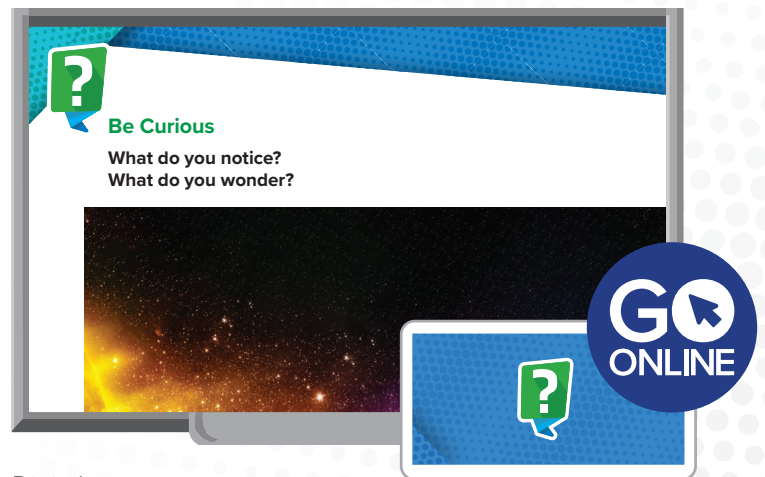
Be Curious, written by Annie Fetter, launches each session using a high ceiling, low floor sense-making activity with multiple entry points to help create an equitable classroom culture where all ideas are welcome and respected.



Print



Annie Fetter
Contributing Author



Digital

Number Routines

More or Less Than

Students build fluency with estimation strategies as they determine whether the value of a given expression is more or less than the target number.

These prompts encourage students to talk about their estimates:

- What numbers helped you think about your solution?
- How did you reason about the results?
- How does your strategy compare to ___'s?

More or Less Than...

In this routine, students estimate a result using any strategy and then compare their estimate to a given value. The intent is for them to estimate results rather than determine the exact result.



Number String Matrix

Students build fluency with operations as they use the solution to an equation to solve equations with the same digits with different base ten values.

These prompts encourage students to talk about their estimates:

- How are the factors related in the rows or columns?
- How does knowing $[9] \times [5]$ help you think about $[90] \times [500]$?
- What new problems could you solve because you know $[9] \times [5]$?

Number String Matrix

A Number String is a list of related equations. Students use the solution strategy for the first equation to solve the subsequent equations. A number string matrix is a set of related problems that are presented in rows and columns. Students pick a row or a column and solve the equations.



Number Routines

Authored by John SanGiovanni, M.Ed., **Number Routines** appear throughout the program to build number sense and proficiency, helping students fluently and flexibly apply strategies to solve problems.



**John SanGiovanni,
M.Ed.**

Contributing Author

Mathematical Discourse

Throughout the program, students have the opportunity to engage in discussion about the math concepts from the lesson to build deeper understanding.

Orchestrating Rich Mathematical Discourse

In this lesson, students are introduced to and explore concepts related to ratio reasoning, a big idea in middle school mathematics. It's important that students have opportunities to engage in discussion about these concepts as they build their understanding of them. These suggestions from can help optimize the discussion of ratio concepts during either the Activity-Based or Guided Exploration.

1. Anticipate likely student responses.

- Activity-Based Exploration: As you plan for the lesson, think about the strategies your students are likely to use and misconceptions some students may have.
- Guided Exploration: As you plan for the lesson, review the questions in the teacher presentation and anticipate student responses to those questions. Think about which questions may pose challenges for students.

5 Practices for Orchestrating Productive Mathematical Discourse

Smith and Stein (2011)

1. **Anticipate** likely student responses.

2. **Monitor** students' thinking

3. **Select** student thinking to feature

4. **Sequence** student responses

5. **Connect** student thinking

Build Understanding Through Exploration

Teachers have their choice of two instructional strategies to facilitate student learning during the **Explore & Develop** phase:

Activity-Based Exploration

Students work together to explore concepts, develop and test hypotheses, and—most importantly—engage in productive struggle as they problem solve and generalize learning. Options for hands-on or digital activities are provided.

Guided Exploration

Teachers facilitate exploration through thoughtful discourse and collaboration using an interactive, digital presentation.

The screenshot shows a digital interface for 'Explore - Session 1' (15-20 min). It features two main exploration paths: 'Activity-Based Exploration' and 'Guided Exploration'. The 'Activity-Based Exploration' path includes a 'Dividing with Fractions and Whole Numbers' section with tasks, materials, directions, and support strategies. The 'Guided Exploration' path includes a 'STEM Camp' section with materials, purposeful questions, and collaborative tasks. Both paths include 'Math is...' sections with 'Using Representations' and 'Multilingual Learner Scaffolds' (Entering/Emerging, Developing/Expanding, Bridging/Reaching).

ETP Effective Teaching Practices

MLR Math Language Routines

SMP Standards for Mathematical Practice

MLL Multilingual Learner Scaffolds

How Do I Choose?

Teachers can reference guidance in the Unit Opener or online in the Digital Teacher Center Unit Resources to help them decide which exploration to implement for lessons in a unit. The How Do I Choose? print and digital resources provide considerations for student engagement, scheduling, personal preference, and a variety of pairings or groupings.

How Do I Choose?

To decide which exploration is best for your class, consider the following:



▶ Activity-Based Exploration

- My students need practice working in pairs.
- During the **Be Curious** conversation, my students demonstrated they have the mindset to explore the concept on their own.

▶ Guided Exploration

- My students are engaged during class conversations.
- My students need practice presenting ideas to the entire class.
- My students struggled to see the math in the **Be Curious** conversation and need extra support to make connections during the **Explore & Develop**.



Explore: Activity-Based Exploration

Activity Based Exploration: Proportional Reasoning

Activity Based Exploration: Dog Breed Cards

Guided Exploration: Salt-Water Aquarium

Digital Activity-Based Exploration

Jacob is setting up a salt-water aquarium. The aquarium needs to have a salinity level of 35 grams of salt per kilogram of water ($1000 \text{ cm}^3 = 1 \text{ kg}$).

75,000 cm^3

How much salt will Jacob need to add to the water for the salinity level to be correct?

Jacob needs to add 2,625 grams of salt to the water.

Digital Guided Exploration Presentation

Go Online and Explore!

Log in to the Digital Teacher Center to assign an interactive, digital Activity-Based Exploration to all or selected students. They can record their observations and findings in their Activity Exploration Journal.

If Guided Exploration is more suitable to class needs for the lesson, log in to the Digital Teacher Center to launch an interactive, digital presentation.

Assess to Inform Instruction and Differentiation

Name _____ Date _____ Period _____

Lesson 3-5
Exit Ticket

For item 1, use the information in the tables to complete the exercise.

The ratio tables show the number of red circles that Anna and Ruth each used in a design.

Anna			
Red Circles	3	6	9
Shapes	5	10	15

Ruth			
Red Circles	5	10	15
Shapes	8	16	24

1. Who has the greater ratio of red circles to shapes? Explain how you determined the answer.

Exit Ticket

At the end of Session 1, students demonstrate their understanding of lesson concepts by completing the **Exit Ticket**. Data from the Exit Ticket will help teachers inform instruction for the next session of that lesson.

Name _____

Lesson 3-5
Lesson Quiz

For item 1, use the tables to answer the question.

1. Each table represents an equivalent ratio. Complete the sentences.

Orange Juice			
Size (fl oz)	12	16	32
Cost (\$)	\$1.80	\$2.40	\$4.80

Grapefruit Juice			
Size (fl oz)	8	20	40
Cost (\$)	\$1.44	\$3.60	\$7.20

Based on the cost per fluid ounce, _____ juice is the less expensive drink. It is _____ cents per fluid ounce less expensive.

For item 2, use the graph to answer the question.

2. In the last 30 minutes, a car has traveled at a constant speed of 65 miles per hour on a highway. The graph shows the distance a train has traveled in the last 30 minutes.

Complete the sentence.
The _____ is traveling at a greater constant speed by _____ miles per hour.

For items 3 and 4, use the tables that show the ratio of chilies to all ingredients in two hot sauce recipes.

Recipe 1			
Chilies (g)	3	6	9
All Ingredients (g)	5	10	15

Recipe 2			
Chilies (g)	7	14	21
All Ingredients (g)	12	24	36

3. Which can you use as the second term in the ratio to compare the ratios of both recipes?
A. 24 B. 30 C. 42 D. 60

Lesson Quiz

At the end of Session 2, students complete the Lesson Quiz. Quiz data informs decisions for differentiation using the **Lesson Quiz Skill Tracker**.

Lesson Quiz Skill Tracker

The Lesson Quiz Skill Tracker in the Teacher Edition identifies Depth of Knowledge (DOK) to help teachers determine the next steps for each student based on quiz performance.

Lesson Quiz Skill Tracker

Item	DOK	Skill
1	1	Understand ratio relationships
2	2	Use ratio reasoning
3	2	Use ratio reasoning
4A	1	Understand ratio relationships
4B	3	Use ratio reasoning

Purposeful Practice

Practice & Reflect

Practice & Reflect provides students with opportunities to solidify their understanding of the lesson concepts through independent practice pages. Practice pages can be completed in the Interactive Student eBook or in the print Student Edition. Additional practice exercises are available online in Extra Practice with algorithmic question functionality, which changes question values upon attempt and includes learning aids.

For exercises 5 and 6, use a graph, table, or equation to represent the proportional relationships. Then answer the questions.

5. A bagger at a grocery store earns \$48.75 for working 3 hours. How much would she earn for working 1 hour? 12 hours?

6. At the farmer's market, Hans paid \$3.99 for 3 pounds of bananas. How much would he pay for 5 pounds of bananas?

For exercises 7 and 8, answer the questions.

7. The equation $y = 2.54x$ represents the relationship between centimeters and inches. What is the constant of proportionality and how could you use it to find the number of centimeters in 50 inches?

8. **Error Analysis** The graph shows the fee scale for a cleaning service. A sales representative says that the service charges \$25 per hour for cleaning. What feedback would you give the sales representative?

Reflect
Explain to a classmate how to determine if a relationship is proportional.

Math In... Mindset
Why was it important to explain your thinking clearly and concisely?

Print Practice

Dynamic Practice

Name _____ Date _____ Period _____

Practice

For exercises 1-4, answer the questions.

1. The relationship between the recommended diameter of an exercise hoop and a person's height is shown. How do the diameters compare to the different heights?

Height (in.)	Diameter (in.)
58	29
60	32
62	31
64	32

2. Aspect ratio is the ratio of width to height of a television screen. The table shows the width and height of several different televisions. How does the width to height compare?

Width (in.)	Height (in.)
27.9	15.7
37.5	21.1
43.6	24.5
56.7	31.9

3. The number of points Imani earns while playing a video game is proportional to the number of stars that she collects. The graph of this relationship passes through the points (0, 0) and (2, 600). How can you use the information to determine the number of points Imani earns for collecting one star?

4. **STEM Connection** An engineer is studying the amount of time it takes to charge the battery for three different electric cars and the distance the car can travel on a fully charged battery. Is the relationship between the time and distance proportional? Explain.

Car	Full Charge Time (hours)	Distance on Full Charge (miles)
Car A	8	240
Car B	6	120
Car C	8	200



Dynamic Digital Practice
Lessons include a range of practice sets with interactive question types, helpful tools, hints, examples, and multiple attempts allowed to support student success.

Additional Practice: Compare Ratio Relationships

03-05 Additional Lesson Practice (RM25 C1)

Question 11 of 15

Question 11

Two bicyclists are traveling around the same track. The number of laps completed by bicyclist A and the time it took in minutes is shown in the table. The number of laps completed by bicyclist B and the time it took in minutes is shown in the graph.

Bicyclist A			
Number of laps	2	4	6
Time (in minutes)	5	10	15

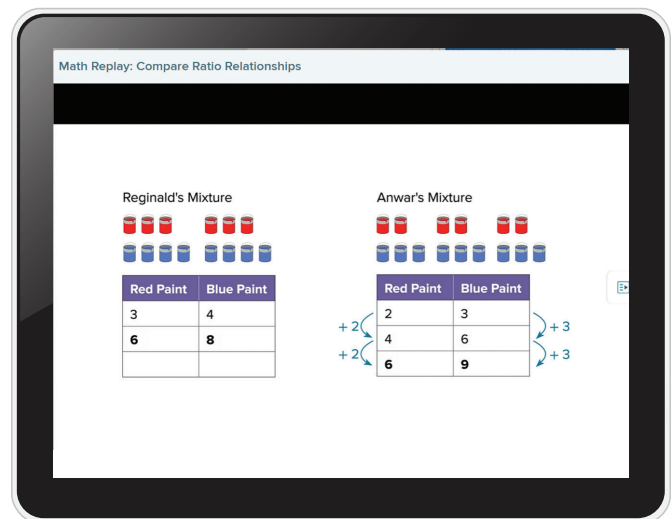
Applied Learning

Students complete exercises related to the lesson content. The exercises for each lesson target students' understanding of the concept or skill, their proficiency (fluency) with the skills, and include opportunities to apply the concepts and skills to new or unfamiliar situations. The section ends with a Reflect question that has students reflect on either the lesson concepts or specific mathematical thinking habits.



Math Replay Videos

A one- to two-minute video explanation of the lesson concept for students to reference as they complete independent practice assignments.



To review today's lesson, have students watch the Math Replay video in their Digital Student Center.


Assign the On My Own practice to students from the Digital Teacher Center.



Differentiation for Diverse Learners

Robust differentiation resources help teachers meet the learning needs of students who would benefit from enrichment to extend learning or provide additional reinforcement for students requiring support.


B Build Proficiency
GO ONLINE
INDEPENDENT WORK



Assign

Interactive Additional Practice

Assign students either the print or digital assignment to practice lesson concepts. The digital assignment includes algorithmic exercises.



Assign

Spiral Review

Assign students either the print or digital version to review these concepts and skills.

- Recognizing Place Values and the Relation to Each Other

Lesson 2.7
Additional Practice

For exercises 1–6, determine whether or not each question is a statistical question.

1. How many minutes does the computer software require each week?
statistical question

2. How many minutes does the computer software require each week?
not a statistical question

3. What are the brand names of athletic shoes on your feet?
statistical question

4. How many minutes does the computer software require each week?
not a statistical question

5. How many minutes does the computer software require each week?
not a statistical question

6. How many minutes does the computer software require each week?
not a statistical question

Lesson 2.8
Spiral Review

For exercises 1–6, determine whether or not each question is a statistical question.

1. How many minutes does the computer software require each week?
statistical question

2. How many minutes does the computer software require each week?
not a statistical question


3. How many minutes does the computer software require each week?
not a statistical question

4. How many minutes does the computer software require each week?
not a statistical question

5. How many minutes does the computer software require each week?
not a statistical question

6. How many minutes does the computer software require each week?
not a statistical question

E Extend Thinking
GO ONLINE
INDEPENDENT WORK



Assign

STEM Adventures

In this STEM Adventure, students display, describe, and analyze data about daily household water consumption. Then they use statistics to investigate how water consumption is affected by wasteful or conserving behaviors and compare data sets.

Lesson 2.8
Extend Thinking

For exercises 1–6, identify whether the question is statistical or not statistical. Then rewrite the question as it is in the other type. For example, if the question is statistical, rewrite the question so that it is not statistical.

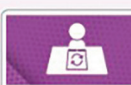
1. In which year did Seattle have the most rainfall?
not statistical
Answers will vary. Sample answer: What was the yearly rainfall in Seattle for each year over the last 50 years?

2. What is your favorite flavor of ice cream?
statistical
Answers will vary. Sample answer: How many cups of ice in a pint of ice cream?

3. How many voters are in your local county?
statistical

4. How many feet tall is the Empire State Building?
not statistical

R Reinforce Understanding
GO ONLINE
INDEPENDENT WORK



Assign

Take Another Look Lessons

Assign the interactive lessons to reinforce targeted skills.

- Statistical Questions
- Create Line Plots and Dot Plots
- Describe a Data Distribution

Lesson 2.8
Reinforce Understanding

Statistical questions have variability in the responses. If a question does not have variability, then it is not statistical.

Determine whether or not each question is a statistical question.

<p>How many states are in the United States? not statistical</p> <p>There are 50 states in the United States. This is a fact because the number is the same for everyone. The number of states in the United States is always going to be 50. Because there is no variability in the responses, this question is not statistical.</p>	<p>How many states have you visited? statistical</p> <p>Everyone who lives in the United States is likely to have visited a different number of states. It is possible to answer this question for every person. This shows that the question has variability in the responses. So, this is a statistical question.</p>
--	--

For exercises 1–6, determine whether or not each question is a statistical question. Write statistical or not statistical.

1. What is your favorite color?
not statistical

2. How many 6th graders at this school are being taught?
not statistical

3. How tall is the Statue of Liberty?
not statistical

4. How many hours a day do you spend on social media?
statistical

5. How many children of each age live in your town?
statistical

6. How many hours a day do you spend on social media?
statistical

For exercises 7 and 8, change the question so that it is a statistical question.

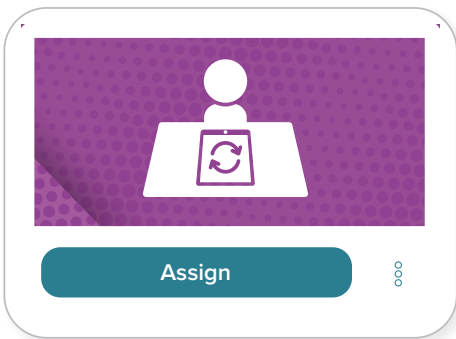
7. How many children of each age live in your town?
Answers will vary. Sample answer: What is the average rainfall for each region of the United States each month?

8. What are the temperatures at each hour in Denver, Colorado?
Answers will vary. Sample answer: What was the temperature at the top of the hour each hour yesterday?

Lesson Walkthrough *Minnesota Reveal Math 6–8* | 29

Enrich Learning with Differentiated Resources

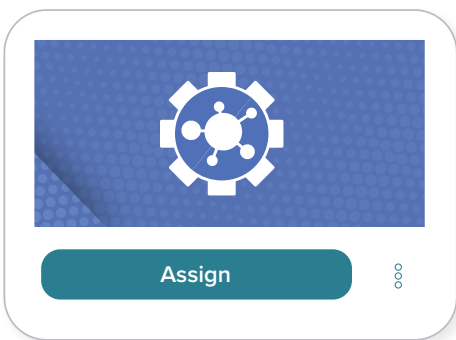
Minnesota Reveal Math® offers a variety of engaging, multimodal activities with different delivery options to meet the individual needs of all students.



Take Another Look

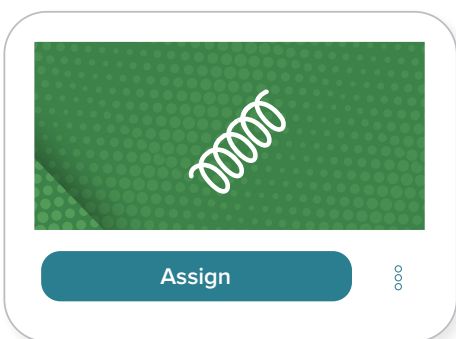
On-Level Reteach Mini-Lessons

Self-paced, digital mini-lessons consist of a three-part, gradual release activity: Model, Interactive Practice, and Check.



Extend Thinking Activities

Extend Thinking Activities challenge students who are ready to learn more. STEM Adventures is one Extend Thinking activity that involves students conducting experiments, making hypotheses, and analyzing data.



Spiral Review

Use the Spiral Review assignments at the end of a lesson to practice concepts presented in prior lessons.



Digital Game Center

Digital Games help students become proficient with grade-level concepts in a fun and engaging practice environment.

Support for Multilingual Learners

In addition to Multilingual Language Scaffolds found in the Teacher Edition, *Minnesota Reveal Math* includes an English/Spanish glossary to assist multilingual learners as they build language and mathematical proficiency:

Math Language Development

Minnesota Reveal Math is rife with mathematical language and specialized terms that may be new to students. Built-in academic language and text features help them grow their mathematical vocabulary and master key terms they are expected to know.

Math Language Development

Language Development - Academic Language

These mini-lessons focus on the academic terms listed in the Unit 3 planner.

Emerging/Entering

Write this sentence on the board and then read them aloud for the group.

*There are about [500] people in the photo on the Unit opener. Ask: Do we know the number of people in the photo? [No]. We can make a guess. A guess is an **estimate**. Let's estimate the number of [leaves on a tree/stars in the sky/people in a stadium]. Have students use this sentence frame: I estimate the number of... to be... Students can ask one another questions that lend themselves to estimates, such as, "Can you estimate the cost of...?" "I estimate the cost to be..."*

Developing/Expanding

Direct students to the Be Curious image in Lesson [x-x]. Say, *Let's analyze the different springs. What do we do when we **analyze** something? [We look closely at it.] What kinds of statement might we make when analyzing the springs? [the number of values in each category]* Write down students' ideas on the board or white board. Then have students work with a partner to analyze the data and then share out with the groups.

Bridging/Reaching

Display these two words: **estimate** and **predict**. Have students decide whether the statements below reflect estimating or predicting.
*If I want to buy new sneakers and headphones, I'll need about \$200.
I think our team will win the game tomorrow.
It will probably take us 40 minutes to run 5 miles.*

Have students discuss the difference between estimating and predicting.

Math Probes by Cheryl Tobey

Target Common Misconceptions

Math Probes, written by Cheryl Tobey, a leading expert in formative assessment, are designed to uncover students' mathematical misconceptions. These formative assessments, placed at the point-of-use in every unit, allow teachers to make sound instructional choices while teaching students that mistakes are an opportunity for growth.



Cheryl Tobey, M.Ed.
Contributing Author

Short, Formative Assessment

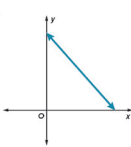
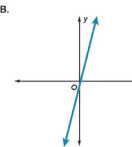
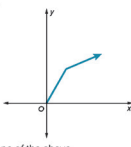
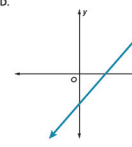
Each **Math Probe** features three to four items that assess students' conceptual understanding. Each item consists of two parts:

- **Part One** assesses students' understanding of concepts.
- **Part Two** asks students to share their thought process and ideas.

Name _____ Date _____ Period _____

Proportional Relationships

Circle the item(s) in each exercise that show a proportional relationship. You may select more than one item. Select none of the above if none of the items show a proportional relationship.

Circle your choice(s).	Explain your choice(s).
<p>1.</p> <p>A. $c = 3.75n$</p> <p>B. $p = 4m$</p> <p>C. $x = y$</p> <p>D. $y = x + 4$</p> <p>E. none of the above</p>	
<p>2.</p> <p>A. </p> <p>B. </p> <p>C. </p> <p>D. </p> <p>E. none of the above</p>	

Circle the item(s) in each exercise that show a proportional relationship. You may select more than one item. Select none of the above if none of the items show a proportional relationship.

Circle your choice(s).	Explain your choice(s).																														
<p>3.</p> <p>A. Aiden and Isabella are running at the same rate around a track. Isabella had already run 4 laps before Aiden started. How many laps had Aiden run after Isabella had run n laps?</p> <p>B. Riley can type 30 words in 14 seconds on her phone. At this rate, how many words can she type in m minutes?</p> <p>C. Javier paints 50 square feet in 125 hours. How long will it take Javier to paint x square feet?</p> <p>D. none of the above</p>																															
<p>4.</p> <p>A. <table border="1" data-bbox="779 1533 974 1585"> <tr><td>Time (h)</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> <tr><td>Number of Items</td><td>4</td><td>8</td><td>12</td><td>16</td></tr> </table></p> <p>B. <table border="1" data-bbox="779 1585 974 1638"> <tr><td>Number of Items</td><td>2</td><td>4</td><td>6</td><td>8</td></tr> <tr><td>Cost (\$)</td><td>5</td><td>10</td><td>12</td><td>15</td></tr> </table></p> <p>C. <table border="1" data-bbox="779 1638 974 1690"> <tr><td>Gallons</td><td>1</td><td>2</td><td>3</td><td>4</td></tr> <tr><td>Miles</td><td>25</td><td>50</td><td>75</td><td>100</td></tr> </table></p> <p>D. none of the above</p>	Time (h)	1	2	3	4	Number of Items	4	8	12	16	Number of Items	2	4	6	8	Cost (\$)	5	10	12	15	Gallons	1	2	3	4	Miles	25	50	75	100	
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Miles	25	50	75	100																											

Take Action

The teacher support materials that accompany the **Math Probes** are designed around a three-part ACT cycle:

- **Analyze** the probe.
- **Collect** and assess student work.
- **Take Action** to correct misconceptions quickly and efficiently.

Math Probe

A

Analyze the Probe ✓ Formative Assessment

Review the probe prior to assigning it to your students. In this probe, students will determine which item(s) in each set show a proportional relationship and explain their choices.

Targeted Concept Understand proportional relationships in equations, tables, and verbal descriptions in which there is a constant ratio between two quantities.

1. Targeted Misconceptions

- Students may not recognize a proportional relationship when given a form other than $y = mx + 0$.
- Students may incorrectly assume that any graph that forms a straight line is proportional.

Authentic Student Work

Below are examples of correct student work and explanations.

Correct Example A

Set 4	a)	Time (hour)	1	2	3	4	5	6
		Number of Items	0	4	8	12	16	
	b)	Number of Items	2	4	6	8		
		Cost (\$)	0	5	10	12	15	
			2.5	4.2	6.1	7.10		
			2.5	4.3	1	2.10		
	c)	Gallons	1	2	3	4		
		Miles	0	25	50	75	100	
			25	50	75	100		
	d)	none of the above						

a + c are both through (0,0) and constant rate.
b doesn't seem to have a constant rate that I can find.

Correct Example B

Set 1	a)	$c = 3.75n$	$c = 3.75n$
	b)	$p = 4m$	$0 = 3.75(0)$
	c)	$x = y$	$0 = 0$
	d)	$y = x + 4$	$p = 4n$
	e)	none of the above	$0 = 4(0)$
			did (c,p) test
			$x = y$
			$0 = 0$
			$y = x + 4$
			$0 = 0 + 4$
			$0 = 4$

C

Collect and Assess Student Work

IF the student selects...	THEN the student likely...	Sample Misconceptions
1. d. Does not select a, b, and/or c	does not understand that for a relationship to be proportional, y must equal 0 when $x = 0$, or may not recognize a proportional relationship when given a form other than $y = mx + 0$.	
2. a and/or d	assumes that all linear relationships are proportional.	In this case, the student includes linear relationships shown in a and d.
3. a and/or c	assumes that a constant rate of change automatically implies a proportional relationship.	In this case, the student assumes a constant rate for square feet per minute.
4. b or d; Does not select a and/or c	does not understand that for a relationship to be proportional, each ratio has the same unit ratio.	
*Combinations of correct and incorrect responses	Many of the above difficulties result in a combination of correct and incorrect responses. For correct responses, be sure to check for sound reasoning.	

T

Take Action

- Choose from the following resources or suggestions.
- Provide opportunities for students to see the same proportional context in a variety of representations in order to make connections between the various components of each representation in Lesson 5.
- Have students compare and contrast proportional relationships with non-proportional relationships to help them generalize the characteristics of a proportional relationship. Focus on the key features of the proportional relationships in Lesson 3.
- To help solidify concepts, have students create, represent algebraically, solve, and share their own problems involving contexts of proportionality in Lessons 4 and 5. This gives students the opportunity to observe key features in others' representations.

- Technology can enhance learning opportunities and allow students to concentrate on the connections between the various representations. Students will begin to see that key features of a graph look different based on the form of the written equation in Lesson 3.
- Revisit the Probe** After additional instruction, have students review their initial answers to the probe. Use these questions for discussion.
 - What answers, if any, would you like to change? Why might you want to change them?
 - What questions do you still have about any of the items in this probe?

Unit Review

Resources for Assessment Preparation

Teachers can select the appropriate review activities to prepare students for unit assessments.

Name _____ Date _____ Period _____

Unit Review

Revisit the **What Do I Already Know?** page and complete the **After** section of the chart.

Vocabulary Activity

Use the words from the word bank to complete each sentence. Some words may be more than once.

- constant of proportionality
- nonproportional
- proportion
- proportional
- proportional relationship
- ratio
- unit rate

- In a proportional relationship, the constant ratio is called the _____.
- Two quantities that do not relate by a constant multiple are _____.
- The relationship between two quantities is _____ if the ratios comparing the two quantities are equivalent.
- The constant of proportionality is also the _____.
- A _____ is an equation stating that two ratios or rates are equivalent.
- A _____ is a comparison between two quantities, in which for every a units of one quantity, there are b units of another quantity.
- There is no _____ in a nonproportional relationship.
- Two quantities are in a _____ if the two quantities vary and have a constant ratio between them.

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Students can use the **Vocabulary Activity** in the Student Edition to review mathematical language and terminology.

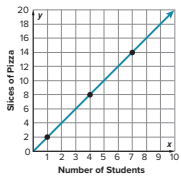
Review

For exercises 9-10, solve each problem.

- Last week, Karen sold 15 bracelets and made a profit of \$71.25. Assuming her costs and selling price stay the same, how much profit will she make from selling 25 bracelets? (Lesson X)
- Approximately how many pounds does a 2-kilogram jellyfish weigh? Round your answer to the nearest tenth. (Lesson X)

For exercise 11, select all statements that are true.

- The relationship between the number of slices of pizza purchased and the number of students served is shown in the graph. Which of the statements are true? (Lesson X)



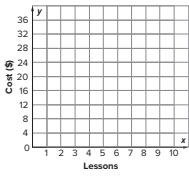
- The relationship is proportional.
- The point (9, 18) satisfies this relationship.
- The constant of proportionality is $\frac{1}{2}$.
- The constant of proportionality is 2.
- The graph shows that every two student had one piece of pizza.

For exercises 12-13, use the scenario below.
Mrs. Jameson paid \$202.50 for a group of 9 students to visit an amusement park.

- Write an equation that can be used to determine the cost for x students to visit the amusement park. (Lesson X)
- What would be the total cost if four more students wanted to join the group? (Lesson X)

For exercises 14-15, use the scenario below.
The cost of dance lessons is \$12 for 1 lesson, \$22 for 2 lessons, and \$32 for 3 lessons.

- Graph the ordered pairs on the coordinate plane. (Lesson X)



- Is the cost of dance lessons proportional to the number of lessons? Explain your reasoning. (Lesson X)

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Review exercises prepare students for assessments with practice targeted to mathematical content standards.

Item Analysis Tables in the Teacher Edition align lesson content to Depth of Knowledge (DOK) levels for each item.

Review

Item Analysis

Item	DOK	Lesson
9	2	2-1
10	2	2-1
11	2	2-5
12	3	2-2
13	2	2-4
14	2	2-4
15	2	2-2

Fluency Progression and Practice

The Fluency Objective and Progression at the close of each unit helps teachers evaluate student progress. Fluency Practice provides students with opportunities to build procedural fluency.

Build Fluency Objective Students build fluency with division with multi-digit decimals. As students work to develop fluency with division with multi-digit decimals, have them reflect on and share with classmates the strategies they find the most useful.

Fluency Progression

Unit	Skill
1	Division with Multi-Digit Decimals
2	Fraction Multiplication and Division (no negative rational numbers)
3	Apply Operations with Multi-Digit Decimals
4	Finding Unit Rates Including Terms with Fractions
5	Percent Increase and Percent Decrease
6	Equations in Proportional Relationships
7	Adding and Subtracting Positive and Negative Rational Numbers
8	Multiplying and Dividing Positive and Negative Rational Numbers
9	Two-Step Equations ($px + q = r$)
10	Solving $p(x + q) = r$

1. Fluency Strategy

Students review the mathematical strategies.

2. Fluency Check

Students complete the practice.

3. Fluency Talk

Students explain the mathematical strategy.

Name _____ Date _____ Period _____

Fluency Practice

Fluency Strategy

Add or subtract decimals.

Align the decimal points. Annex zeros, if needed. Add or subtract as with whole numbers.

$$\begin{array}{r} 1 \\ 4.560 \\ + 13.246 \\ \hline 17.806 \end{array} \qquad \begin{array}{r} 6 \text{ } 10 \\ 26.7\cancel{0} \\ - 3.45 \\ \hline 23.25 \end{array}$$

Multiply decimals.

Multiply. To place the decimal point, find the sum of the number of decimal places in each factor. The product has the same number of decimal places.

$$\begin{array}{r} 3.4 \\ \times 0.56 \\ \hline 204 \\ + 1700 \\ \hline 1.904 \end{array}$$

Divide decimals.

Multiply both the divisor and dividend by a power of 10 so that the divisor is a whole number. Divide. Place the decimal in the quotient directly above the decimal in the dividend.

$$\begin{array}{r} 3.4 \\ 1.2 \overline{) 4.08} \\ \underline{-36} \\ 48 \\ \underline{-48} \\ 0 \end{array}$$

1

2

3

Fluency Check

Add, subtract, multiply, or divide.

- $5.1 + 8.2 =$ _____
- $7.68 - 1.49 =$ _____
- $2.3 \times 1.4 =$ _____
- $55.9 \div 13 =$ _____
- $2.74 + 3.029 =$ _____
- $2.5 - 0.586 =$ _____
- $0.85 \times 0.09 =$ _____
- $3.6 \div 0.09 =$ _____

Fluency Talk

How would you describe the differences between operations with whole numbers and operations with decimal numbers to a classmate?

Unit Review

Performance Task

For Part A through C, answer the question and include justifications.

Miranda and Juan want to rent bicycles for the afternoon. They will rent from either City Cycles or Biking Adventures. The rental rates are shown in the posters.

Part A

Which company should they rent from if they plan to rent bicycles for 2 hours or less?



Part B

Which company should they rent from if they plan to rent bicycles for 5 hours or less?



Part C

Miranda and Juan decide to rent for 3 hours. They find out that City Cycles charges a flat fee of \$2.50 to rent a bicycle helmet, but Biking Adventures includes helmet rental in the rental cost. From which store should they rent if they want to pay the lower price?

Unit Reflect

What helps you recognize a proportional relationship?

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Performance Task

Each unit culminates in two Performance Tasks that challenge students to apply skills from the current unit in real-world settings.

For each unit, one Performance Task is available in the Student Edition. A second, secure Performance Task is available in the Teacher Digital Center for use as an assessment. Teachers can navigate to the Assess section for the specific unit to assign the Performance Task.

Mathematical Modeling

The Mathematical Modeling tasks wrap up each unit with a real-world scenario related to the STEM unit focus and incorporating the Standards for Mathematical Practice. Students are provided with the opportunity to model with mathematics while utilizing appropriate tools to solve real-world problems and constructing viable arguments to present to their peers.

Students can choose between two different projects, increasing engagement and developing student agency. Teacher support is provided, including a guide for project development and facilitation.

Name _____ Date _____ Period _____

Mathematical Modeling

Measuring and Comparing Air Quality

The Air Quality Index (AQI) is a scale that informs the public on the quality of the air for the day. The AQI looks at five different pollutants in the air to determine air quality.

Air Quality Index (AQI) Values	Levels of Health Concern
0 to 50	Good
51 to 100	Moderate
101 to 150	Unhealthy to Sensitive Groups
151 to 200	Unhealthy
201 to 300	Very Unhealthy
301 to 500	Hazardous

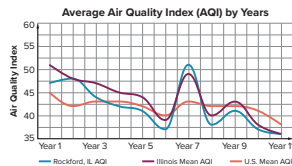
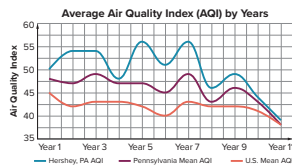
Choose one of the projects to complete.

Project One

The U.S. Olympic Committee is planning to build a new training facility for the track and field team. The committee is considering two possible locations: Hershey, Pennsylvania or Rockford, Illinois. Among the considerations for the new site is the average air quality. Good air quality is important for athletes, especially runners.

The graphs show the average air quality index for each site over a period of 11 years.

You are part of the site selection team and your team will make a recommendation to the U.S. Olympic Committee. Your task is to analyze the data in the graphs for the team. Consider the change in air quality over the ten-year period, noting any trends that you think might continue. Also consider the differences in the air quality for each specific site, for the state in which the site is located, and the country.



Project Two

The superintendent in your school district has received a complaint of poor indoor air quality in one of the district schools. Four key indicators of indoor air quality with maximum acceptable levels are described in the table.

Pollutant	Source	Level
Carbon Dioxide (CO ₂)	Exhaled air from human breathing; combustion processes of carbon fuels	< 1,000 parts per million (ppm)
Carbon Monoxide (CO)	Improperly vented furnaces, malfunctioning gas ranges.	< 9 ppm
Particle Pollution PM ₁₀	Particulates with a diameter of 10 micrometers or less. Includes dust from soil, pollen, mold, burning of wood, oil, or coal	< 50 mg/m ³ for one hour
Particle Pollution PM _{2.5}	Particulates with a diameter of 2.5 micrometers or less. Includes soot from diesel engines in trucks and buses	< 12.0 mg/m ³

The superintendent has asked you and your classmates to analyze the results of the air quality tests. What do the results shown in the table suggest about the indoor air quality at the school in question?

Pollutant	Reading 1	Reading 2	Reading 3	Reading 4
Carbon Dioxide (CO ₂)	729 ppm	1030 ppm	956 ppm	1106 ppm
Carbon Monoxide (CO)	4 ppm	5 ppm	3 ppm	5 ppm
Particle Pollution PM ₁₀	52 mg/m ³	56 mg/m ³	62 mg/m ³	58 mg/m ³
Particle Pollution PM _{2.5}	10 mg/m ³	10 mg/m ³	9 mg/m ³	10 mg/m ³

Flexible Assessments for Growth

Minnesota Reveal Math[®] assessments allow students to demonstrate understanding through multimodal responses—verbal, written, visual, and hands-on. Assessments were designed with **Universal Design for Learning (UDL)** principles to support flexible, inclusive, and meaningful assessment.

Diagnostic Insights

Measure student understanding of prerequisite skills at the start of the year and before each unit with:

- The *ALEKS* Initial Knowledge Check—administered digitally at the beginning of the year.
- Unit Readiness Diagnostics—available in print or digital formats.

Summative Assessments and Performance Tasks

Evaluate student understanding, application, and progress aligned with the Minnesota Mathematics Standards through:

- Unit Assessments
- Unit Secure Performance Tasks

Targeted Intervention

Access ready-made intervention resources aligned to diagnostic and summative assessment results:

- **Guided Support:** Teacher-facilitated, small-group mini-lessons
- **Skills Support:** Skill-based practice for targeted review
- **Take Another Look:** Digital mini lessons with gradual release activities

Name _____


Unit 3
How Ready Am I?


1. Which number makes the equation true?
 $5 + 4 = 4 + ?$
A. 3 B. 4 C. 5 D. 6

2. Cara bought a package of toy cars for each of her 5 friends. Each package has 4 cars. Which equation can be used to find the total number of cars Cara bought?
A. $5 + 4 = ?$ C. $4 + 4 + 4 + 4 = ?$
B. $5 + 5 + 5 + 5 + 5 = ?$ D. $4 + 4 + 4 + 4 + 4 = ?$

3. Marco has 3 shelves in his room. There are 3 trophies on each shelf. How many trophies does Marco have?
A. 3 B. 6 C. 9 D. 12

4. Maria's dog buried 15 bones. Maria found 6 bones. Maria wrote the subtraction equation $15 - 6 = ?$ to find out how many bones are still buried. Which equation could Maria use to help solve her equation?
A. $15 + 6 = 9$ C. $6 - 15 = 9$
B. $6 + 9 = 15$


Readiness Diagnostic

 **Administrator Reports:**
Access key insights and assessment results with ease.

Actionable Insights to Track Progress

The *Minnesota Reveal Math* data system, powered by the **Standards and Skills Graph**, serves as the hub for real-time class and student performance insights, tracking progress over time and highlighting past achievements across grade levels.

Two Inner Rings represent data from interim assessments. This nationally normed data is updated throughout the year and tracks overall student progress by grade and domain.



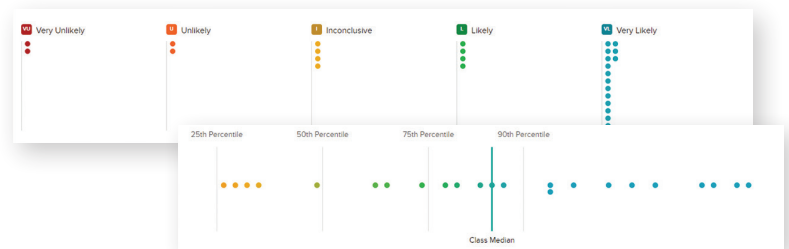
Two Outer Rings display students' proficiency in standards and skills within a specific domain or strand, updated daily with data from *Minnesota Reveal Math* assessments, practice, *ALEKS*®, and intervention data from McGraw Hill's *Number Worlds*®.

Data Sources:

The **Standards and Skills Graph** is populated with student interim assessment data as well as data from McGraw Hill's core, supplemental, and intervention programs.



Distribution Charts provide real-time insights into student readiness, displaying performance data by grade, domain, and standards at a glance. Each dot represents a student's progress, simplifying lesson planning and guiding instruction.



Five Levels of Tailored Recommendations at Your Fingertips

All data captured in the Standards and Skills Graph automatically groups students and generates up to five levels of tailored recommendations, including personalized practice and small-group mini-lessons. Built-in support for intervention and acceleration is all assignable with a single click.

➔ Pre-Requisite
🔄 Reinforce
🎯 On-Lesson
⊕ Extension
➔ Post-Requsite

Explore More Reports Unlock additional insights to support student growth and instruction with:

✓ **Actionable Insights to Track Progress:**
Review real-time data for *Minnesota Reveal Math* practice and assessments, including item analysis by student and class.

✓ **Standards Performance Report:**
See class and student performance by standard, with cumulative scores to support instructional decisions.

Personalize Student Learning Like Never Before

Minnesota Reveal Math® is more than just a curriculum—it's a complete learning ecosystem personalized to meet each student's needs.



Minnesota Reveal Math Generates Rich Data in Real Time

As students answer questions, data from **Interim Assessments, Daily Core Practice & Assessment, Advanced Adaptive Learning, and Dynamic Personalized Practice** flows into the program's data system, generating powerful insights.



Real-Time Data Powers Personalized Learning Paths

Rich data automatically generates individualized learning paths for each student, grouping them by what they need and saving teachers valuable planning time.

As students' needs evolve, the program updates its personalized recommendations accordingly—new data generates new insights each and every day.

Dynamic Personalized Practice A B

Using real-time insights, *Minnesota Reveal Math* automatically groups students and generates up to five levels of personalized recommendations to meet each student's needs. Teachers can easily assign mini-lesson, tools, and scaffolds with one click, ensuring all learners access grade-level content.

Advanced Adaptive Learning with ALEKS® C

ALEKS, embedded within *Minnesota Reveal Math*, uses AI to assess and adjust in real time, providing practice tailored to each student's skill level. This targeted intervention or acceleration helps students focus on what they're ready to learn instead of standard grade-level content.

Collaborative and Independent Learning D

Students apply their understanding through both digital and hands-on small-group activities and independent practice, including ready-made games and tasks with STEM connections.



Minnesota Reveal **MATH**[®]



Learn more at
mheducation.com/minnesota